

http://www.math.csusb.edu/faculty/stanton/m262/intro_prob_models/intro_prob_models.html

Probability distribution for tossing 2 coins.

x	HH	HT or TH	TT
P(x)	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{1}{4}$

<http://regentsprep.org/Regents/math/tree/Ltree.htm>

Independent events: knowing A occurred doesn't tell us any additional information about B.

Disjoint events: A and B can't both happen.

ActivStats III 14-2 Independence

Events A & B are independent if
 $P(A) = P(A|B)$

One trial: Rolling one die...

	Disjoint	Not Disjoint
Independent	Impossible	even & curved number 2, 3, 5, 6
Not Independent	2, 4, 6 even & 1, 3, 5 odd	even & prime 2, 3, 5

2, 4, 6 $P(E) = \frac{3}{6} = \frac{1}{2}$
 $P(\text{curved}) = \frac{4}{6} = \frac{2}{3}$
 $P(E | \text{curved}) = \frac{2}{4} = \frac{1}{2}$

$P(\text{prime}) = \frac{3}{6} = \frac{1}{2}$
 $P(E | \text{prime}) = \frac{1}{3}$
 $P(\text{prime} | \text{even}) = \frac{1}{3}$

Two trials:

$P(E) = \frac{1}{2}$
 $P(E | O) = \frac{0}{3}$

	Disjoint	Not Disjoint
Independent	Impossible	heads on a coin & 6 on a die
Not Independent	Dem elected Pres & GOP elected VP	raining & playing baseball

$P(H) = \frac{1}{2}$
 $P(H | 6) = \frac{1}{2}$

Word order matters!

$P(\text{girl}|\text{has a pink phone}) \neq P(\text{has a pink phone}|\text{girl})$

What is the probability...

a person is a Canadian who speaks French?

a Canadian speaks French?

a person is Canadian if he speaks French?

a person speaks French if he is Canadian?

I flip a coin 3 times. What is the probability I get at least one head?

$P(\text{HHH}) = \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{8}$

$P(\text{HHT}) = \frac{1}{8}$

$P(\text{HTH}) = \frac{1}{8}$

THH

HTT

THT

TTH

TTT

This
IS
better

add = $\frac{7}{8}$

Hi Stats

5th hour

Morgan poops

Canadians

$P(\text{TTT}) = \frac{1}{8}$

$1 - \frac{1}{8} = \frac{7}{8}$

Hi Its hand
Stats to
class write
with a
mouse

I roll a die 3 times. What is the probability I get at least one 4?

$$P(444) = \frac{1}{6} \cdot \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{216}$$

$$P(444^c) = \frac{1}{6} \cdot \frac{1}{6} \cdot \frac{5}{6} = \frac{5}{216} \cdot 3 = \frac{15}{216}$$

44^c4
 4^c44

$$P(44^c4^c) = \frac{1}{6} \cdot \frac{5}{6} \cdot \frac{5}{6} = \frac{25}{216} \cdot 3 = \frac{75}{216}$$

4^c44^c
 4^c4^c4

$$P(4^c4^c4^c) = \frac{5}{6} \cdot \frac{5}{6} \cdot \frac{5}{6} = \frac{125}{216}$$

$$\begin{array}{r}
 + \\
 \hline
 \frac{91}{216} \\
 1 - \frac{125}{216}
 \end{array}$$

Suppose a test for a genetic disorder is 95% accurate and that 10% of the population has the disorder.

What is $P(\text{infected} | \text{positive})$?

