

10.3 Making Sense of Statistical Significance

Some fields have pre-set standards for α .

The P-value describes the strength of evidence, whereas α is a decision making tool.

Person \rightarrow \dots \square α

Large sample sizes often produce statistically significant results, even when the effect is small.

$$z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$$

A U.S. Bureau of Standards inspector weighs a SRS of 50 6 oz. yogurt cups. Yogurt cup weights probably follow a roughly Normal distribution. Checking label accuracy, the inspector tests

$H_0: \mu = 6$ against

$H_a: \mu < 6$

The manufacturer says $\sigma = 0.3$ oz. for the weights.

Is the result significant at the $\alpha = 0.001$ level if the inspector found...

$\bar{x} = 5.9$ oz.?

$p = .009 > .001 = \alpha$
do not reject H_0

$\bar{x} = 5.8$ oz.?

$p = 1.2 \times 10^{-6} < .001 = \alpha$
reject H_0

A researcher writes a new ACT prep course. The researcher tried the new course with a SRS of subjects and found $\bar{x} = 20.2$. That year, nat'l scores were not far from Normal with $\mu = 20$ & $\sigma = 1.2$. The researcher tested

$$H_0: \mu = 20 \text{ against}$$

$$H_a: \mu > 20$$

Find the P-value if the researcher's sample was...

40 students.

$$.15 > \begin{matrix} .05 \\ .10 \\ .01 \end{matrix} \text{ but reject } H_0$$

$\mu = 20$

100 students.

$$.047 < \begin{matrix} .10 \\ .05 \\ .01 \end{matrix} \text{ reject } H_0 \rightarrow \mu > 20$$

but reject

400 students.

$$4.3 \times 10^{-4} < \alpha \text{ reject } H_0$$

$\mu > 20$

.01
.05
.10
.001