

10.7
p. 710

Test will have 4 ?s from
this section like #s 54-86

Apr 4-6:26 PM

Defn $\sqrt{-1} = i$, the imaginary #

then,

$$(\sqrt{-1})^2 = (i)^2$$

$$\boxed{-1 = i^2}$$

we'll need
this when we
simplify expressions.

Apr 4-6:32 PM

ex 8

$$\begin{array}{c} \sqrt{-1} \\ \downarrow \\ -i \end{array} = -i$$

ex 10

$$\begin{aligned} -i^2 &= -1 \cdot i^2 \\ &= -1 \cdot -1 \\ &= (-1)(-1) \\ &= 1 \end{aligned}$$

Apr 4-6:38 PM

ex 12

$$\begin{aligned} &(-i)^2 \\ &= (-1i)^2 \\ &= (-1i)(-1i) \\ &= i^2 \\ &= -1 \end{aligned}$$

ex 14

$$\begin{aligned} &\sqrt{-225} \\ &= \sqrt{-1} \sqrt{225} \\ &= i \cdot 15 \\ &= 15i \end{aligned}$$

Apr 4-6:41 PM

$$\begin{aligned}
 \underline{\text{ex 16}} \quad & -\sqrt{-196} \\
 & = -\sqrt{-1} \sqrt{196} \\
 & = -i \cdot 14 \\
 & = -14i
 \end{aligned}$$

$$\begin{aligned}
 \underline{\text{ex 18}} \quad & \sqrt{-21} \\
 & = \sqrt{-1} \cdot \sqrt{21} \\
 & = i \cdot \sqrt{21} \\
 & \textcircled{i\sqrt{21}} \text{ or } \sqrt{21}i \\
 & \text{or } \sqrt{21}i
 \end{aligned}$$

Apr 4-6:45 PM

$$\begin{aligned}
 \underline{\text{ex 22}} \quad & \sqrt{-3} \cdot \sqrt{-19} \\
 & = \sqrt{-1} \sqrt{3} \cdot \sqrt{-1} \sqrt{19} \\
 & = i\sqrt{3} \cdot i\sqrt{19} \\
 & = i^2 \cdot \sqrt{3} \cdot \sqrt{19} \\
 & = -1 \cdot \sqrt{57} \\
 & \quad -\sqrt{57}
 \end{aligned}$$

$$\begin{aligned}
 \underline{\text{ex 28}} \quad & \frac{\sqrt{-40}}{\sqrt{-10}} = \frac{\cancel{\sqrt{-1}}\sqrt{40}}{\cancel{\sqrt{-1}}\sqrt{10}} \\
 & = \frac{\sqrt{40}}{\sqrt{10}} = \sqrt{\frac{40}{10}} = \sqrt{4} \\
 & \quad = 2
 \end{aligned}$$

Apr 4-6:49 PM

ex 30

$$\frac{\sqrt{-160}}{\sqrt{10}} = \frac{\sqrt{-1} \sqrt{160}}{\sqrt{10}} = i \sqrt{16} = i \cdot 4 = 4i$$

$$\sqrt{-16} = \sqrt{-1} \sqrt{16} = i \sqrt{16}$$

Apr 4-6:55 PM

ex 32

$$\frac{-\sqrt{-100}}{\sqrt{-25}} = -\sqrt{\frac{-100}{-25}} = -\sqrt{4} = -2$$

$$\frac{-\sqrt{-100}}{\sqrt{-25}} = \frac{-i \sqrt{100}}{i \sqrt{25}} = \frac{-i \sqrt{4}}{i} = -\sqrt{4} = -2$$

Apr 4-6:58 PM

ex 34 $(7 + 15i) + (-11 + 14i) = -4 + 29i$

↑ ↑
 real part imaginary part
 complex #s

however

$$(7 + 15i) - (-11 + 14i)$$

$$7 + 15i + 11 - 14i = 18 + i$$

Apr 4-7:02 PM

ex 38 $(9 + i) - (3 + 2i)$

$$= 9 + i - 3 - 2i = 6 - i$$

ex 44 $[(7 + 2i) + (-4 - i)] - (2 + 5i)$

$$= 3 + i - 2 - 5i$$

$$= 1 - 4i$$

Apr 4-7:07 PM

$$\begin{aligned} \underline{\text{ex 48}} \quad (5i)(125i) &= 625 i^2 \\ &= 625(-1) = -625 \end{aligned}$$

$$\underline{\text{ex 50}} \quad (-32i)(-2i) = 64 i^2 = 64(-1) = -64$$

$$\begin{aligned} \underline{\text{ex 52}} \quad & \overset{\curvearrowright}{3i(4+9i)} \\ &= 12i + 27i^2 = 12i + 27(-1) = 12i - 27 \\ &= -27 + 12i \end{aligned}$$

Apr 4-7:12 PM

$$\begin{aligned} \underline{\text{ex 54}} \quad & (7-2i)(3+i) \\ &= 21 + 7i - 6i - 2i^2 \\ &= 21 + i - 2(-1) \\ &= 23 + i \end{aligned}$$

Apr 4-7:17 PM

ex 56

$$(3 + 2i)^2$$

$$= (3 + 2i)(3 + 2i)$$

$$= 9 + 6i + 6i + 4i^2$$

$$= 9 + 12i - 4$$

$$= 5 + 12i$$

$$4i^2 = 4(-1) = -4$$

Apr 4-7:21 PM

ex 62

$$(7 + 2i)(7 - 2i)$$

Conjugates

$$= 49 - 4i^2$$

$$= 49 + 4 \leftarrow -4(-1)$$

$$= 53$$

Apr 4-7:24 PM

ex 64 $(2-i)^2(2+i)^2$

$$(2-i)(2-i)(2+i)(2+i)$$

$$\underbrace{(2-i)(2+i)}_{4-i^2} \cdot \underbrace{(2-i)(2+i)}_{4+i^2}$$

$$5 \cdot 5 = 25$$

Apr 4-7:27 PM

ex 70 Use Conjugates like 10.5

$$\frac{-8i}{1+i} \cdot \frac{1-i}{1-i} \quad \frac{-8}{1+\sqrt{2}} \cdot \frac{1-\sqrt{2}}{1-\sqrt{2}}$$

$$= \frac{-8i + 8i^2}{1-i^2} = \frac{-8i + 8(-1)}{1-(-1)}$$

$$= \frac{-8i - 8}{1+1} = \frac{\overset{4}{-8} - \overset{4}{8}i}{\overset{2}{1}} = -4 - 4i$$

Apr 4-7:33 PM

$$\begin{aligned}
 \underline{\text{ex 72}} \quad & \frac{-38-8i}{7+3i} \cdot \frac{7-3i}{7-3i} \\
 & = \frac{-266+114i-56i+24i^2}{49-9i^2} \\
 & = \frac{-266+58i-24}{49+9} = \frac{-290+58i}{58} \\
 & = -5+i
 \end{aligned}$$

Apr 4-7:39 PM

$$\begin{aligned}
 \underline{\text{ex 74}} \quad & \frac{-1+5i}{3+2i} \cdot \frac{3-2i}{3-2i} \\
 & = \frac{-3+2i+15i-10i^2}{9-4i^2} = \frac{-3+17i+10}{9+4} \\
 & = \frac{7+17i}{13} = \frac{7}{13} + \frac{17}{13}i
 \end{aligned}$$

Apr 4-7:44 PM

ex 76

$$\frac{5-i}{i} \cdot \frac{i}{i} = \frac{5i - i^2}{i^2} = \frac{5i + 1}{-1}$$

$$= -5i - 1$$

$$\frac{5i + 1}{-1} \cdot \frac{-1}{-1} = \frac{-5i - 1}{1}$$

$$= \underline{-1 - 5i}$$

Apr 4-7:49 PM

$$i^3 = i^2 \cdot i = -1 \cdot i = -i \quad \begin{matrix} 4 \sqrt{3} \text{ OR } 3 \\ 1 \text{ R } 0 \end{matrix}$$

$$i^4 = (i^2)(i^2) = (-1)(-1) = 1 \quad \begin{matrix} 4 \sqrt{4} \\ 1 \text{ R } 0 \end{matrix}$$

$$i^{13} = i^{12} \cdot i = i^4 \cdot i^4 \cdot i^4 \cdot i^1 = 1 \cdot 1 \cdot 1 \cdot i = i \quad \begin{matrix} 4 \sqrt{13} \\ 3 \text{ R } 1 \end{matrix}$$

$$i^{18} = i^4 \cdot i^4 \cdot i^4 \cdot i^4 \cdot i^2 = 1 \cdot 1 \cdot 1 \cdot 1 \cdot (-1) = -1 \quad \begin{matrix} 4 \sqrt{18} \\ 4 \text{ R } 2 \end{matrix}$$

Apr 4-7:53 PM

ex 80 $i^{26} = i^2 = -1$ $4 \overline{) 26} \begin{array}{r} 6R2 \\ \end{array}$
ex 82 $i^{48} = i^0 = 1$ $4 \overline{) 48} \begin{array}{r} 12R0 \\ \end{array}$
ex 84 $i^{102} = i^2 = -1$ $4 \overline{) 102} \begin{array}{r} 25R2 \\ \end{array}$
ex 86 $i^{83} = i^3 = -i$ $4 \overline{) 83} \begin{array}{r} 20R3 \\ \end{array}$
ex 88 $i^{-17} = \frac{1}{i^{17}} = \frac{1}{i} \cdot \frac{i}{i}$ $4 \overline{) 17} \begin{array}{r} 4R1 \\ \end{array}$
 $\quad \quad \quad = \frac{i}{i^2} = \frac{i}{-1} = -i$
 $\quad \quad \quad \swarrow$
 $\frac{1}{i^{17}} \cdot \frac{i^3}{i^3} = \frac{i^3}{i^{20}} = \frac{i^3}{1} = i^3 = -i$

Apr 4-8:01 PM