

1.7

ex $13 + 12 = 12 + 13$ commutative

ex $-4 \cdot (2 \cdot 6) = (-4 \cdot 2) \cdot 6$ associative

ex $12 + (-12) = 0$ inverse

ex $-8.456 + 0 = -8.456$ identity

ex $3(5t) - 3(7r) = 3(5t - 7r)$ distributive

$$\begin{aligned}\underline{\text{ex}} \quad & 49 + 199 + 1 + 1 \\ & = 49 + 1 + 199 + 1 \\ & = 50 + 200 \\ & = \textcircled{250}\end{aligned}$$

$$\begin{aligned}\underline{\text{ex}} \quad & 1846 + 1293 + (-46) + (-93) \\ & = 1846 + (-46) + 1293 + (-93) \\ & = 1800 + 1200 \\ & = \textcircled{3000}\end{aligned}$$

$$\begin{aligned}\underline{\text{ex}} \quad & 9r + 12 - 9r + 1 \\ & = 9r - 9r + 12 + 1 \\ & = 0 + 12 + 1 \\ & = \textcircled{13}\end{aligned}$$

$$\begin{aligned}\underline{\text{ex}} \quad & \left(\frac{4}{5}\right)(-.73)\left(\frac{5}{4}\right) \\ & = \left(\frac{4}{5}\right)\left(\frac{5}{4}\right)(-.73) \\ & = (1)(-.73) \\ & = \textcircled{-.73}\end{aligned}$$

$$\begin{aligned}\underline{\text{ex}} \quad 6(11+8) &= 6(11) + 6(8) \\ &= 66 + 48 \\ &= \textcircled{114}\end{aligned}$$

$$\begin{aligned}\underline{\text{ex}} \quad -11(x+4) &= (-11)(x) + (-11)(4) \\ &= -11x + (-44) \\ &= \textcircled{-11x - 44}\end{aligned}$$

$$\begin{aligned}\underline{\text{ex}} \quad -9(g-4) &= (-9)(g) + (-9)(-4) \\ &= \textcircled{-9g + 36}\end{aligned}$$

$$\underline{\text{ex}} \quad 4s + 4r = 4(s + r)$$

$$\underline{\text{ex}} \quad 13(5w) + 13(4p) = 13(5w + 4p)$$

$$\underline{\text{ex}} \quad 9p + 18 = 9p + 9(2) = 9(p + 2)$$

$$\underline{\text{ex}} \quad -(9x + 12y) = -9x - 12y$$

$$\underline{\text{ex}} \quad -(-13x - 15y) = 13x + 15y$$

1.8 like terms - same combination of variables
and exponents

$$\begin{array}{c} \text{exponent} \\ \swarrow \\ 3 \times x^2 \\ \nwarrow \\ \text{variable} \\ \uparrow \\ \text{coefficient} \end{array}$$

ex $8 + 3(s - 6t) = 8 + 3s - 18t$
no like terms

$$\underline{\text{ex}} \quad -10 - (7 - 14r)$$

$$= \underline{-10 - 7} + 14r$$

$$= \downarrow -17 + 14r$$

ex $-23y$ coefficient is -23

ex $9z$ " " 9

ex $-t$ " " -1

ex 98 " " 98

$$\underline{\text{ex}} \quad 15m + 12m = 27m$$

$$\underline{\text{ex}} \quad -3z - 9z = -12z$$

$$\underline{\text{ex}} \quad 30x + x = 31x$$

$$\underline{\text{ex}} \quad \underbrace{9x + 7} - \underbrace{13x + 12} + \underbrace{8x - 10} = \underbrace{4x + 9}$$

$$\begin{aligned} \underline{\text{ex}} \quad & -3(2t + 4) + 8(2t - 4) \\ & = -6t - 12 + 16t - 32 \\ & = 10t - 44 \end{aligned}$$

ex Six times a number, added to the sum of
the number and six

$$\begin{aligned} & 6x + (x + 6) \\ &= 6x + x + 6 \\ &= \textcircled{7x + 6} \end{aligned}$$

2.1 Linear equation in 1 variable:

$$Ax + B = C$$

(A, B, & C are real #s & $A \neq 0$)

+, -, \times , \div each side by some nonzero #.

$$\begin{array}{l} \underline{\text{ex}} \quad x - 4 = 9 \\ \quad \quad +4 \quad +4 \\ \quad \quad x = 13 \end{array} \quad \text{or} \quad \begin{array}{l} x - 4 + 4 = 9 + 4 \\ \{13\} \end{array}$$

$$\begin{array}{l} \underline{\text{ex}} \quad x + 6 = 10 \\ \quad \quad -6 \quad -6 \\ \quad \quad x = 4 \end{array} \quad \text{or} \quad \begin{array}{l} x + 6 - 6 = 10 - 6 \\ \{4\} \end{array}$$

$$\begin{array}{l} \underline{\text{ex}} \quad y + 15.5 = -5.1 \\ \quad \quad -15.5 \quad -15.5 \\ \quad \quad y = -20.6 \end{array} \quad \text{or} \quad \begin{array}{l} y + 15.5 - 15.5 = -5.1 - 15.5 \\ \{-20.6\} \end{array}$$

$$\begin{array}{l}
 \underline{\text{ex}} \quad 9x - 1 = 8x + 4 \\
 \quad \quad -8x \quad \quad -8x \\
 \quad \quad x - 1 = 4 \\
 \quad \quad \quad +1 \quad +1 \\
 \quad \quad x = 5 \quad \quad \{5\}
 \end{array}
 \quad \text{or} \quad
 \begin{array}{l}
 9x - 1 - 8x = 8x + 4 - 8x \\
 x - 1 = 4 \\
 x - 1 + 1 = 4 + 1 \\
 x = 5
 \end{array}$$

$$\begin{array}{l}
 \underline{\text{ex}} \quad -\frac{2}{7}z + 2 = \frac{5}{7}z \\
 \quad \quad +\frac{2}{7}z \quad \quad +\frac{2}{7}z \\
 \quad \quad 2 = \frac{7}{7}z \\
 \quad \quad 2 = z \quad \quad \{2\}
 \end{array}$$

$$\underline{\text{ex}} \quad -\frac{2}{7}z + 2 = \frac{5}{7}z$$

$$7\left(-\frac{2}{7}z + 2 = \frac{5}{7}z\right)$$

$$-2z + 14 = 5z$$

$$+2z \qquad \qquad +2z$$

$$14 = 7z$$

$$\frac{14}{7} = \frac{7z}{7}$$

$$2 = z \quad \{2\}$$

$$\underline{\text{ex}} \quad 4x + 3x - 6 - 6x = 10 + 3$$

$$x - 6 = 13$$

$$+6 \quad +6$$

$$x = 19 \quad \{19\}$$

$$\underline{\text{ex}} \quad (8r - 3) - (7r + 1) = -6$$

$$8r - 3 - 7r - 1 = -6$$

$$r - 4 = -6$$

$$+4 \quad +4$$

$$r = -2 \quad \{-2\}$$

$$\begin{aligned} \underline{\text{ex}} \quad & 9(2m - 3) - 4(5 + 3m) - 5(4 + m) = -3 \\ & 18m - 27 - 20 - 12m - 20 - 5m = -3 \\ & m - 67 = -3 \\ & \quad +67 \quad +67 \\ & m = 64 \\ & \{64\} \end{aligned}$$

2.2 ex $7x = 56$

$$\frac{7x}{7} = \frac{56}{7}$$

$$x = 8 \quad \{8\}$$

ex $5k = -70$

$$\frac{5k}{5} = \frac{-70}{5}$$

$$k = -14 \quad \{-14\}$$

ex $5x = 0$

$$\frac{5x}{5} = \frac{0}{5}$$

$$x = 0 \quad \{0\}$$

ex

$$\frac{x}{5} = 15$$

$$5 \cdot \frac{x}{5} = 5 \cdot 15$$

$$x = 75 \quad \{75\}$$

$$\underline{\text{ex}} \quad \frac{3}{8}x = 9$$

$$\left(\frac{8}{3}\right) \frac{3}{8}x = 9 \left(\frac{8}{3}\right)$$

$$x = \frac{72}{3} = 24 \quad \{24\}$$

$$\underline{\text{ex}} \quad -\frac{3}{4}k = -21 \quad \left(-\frac{4}{3}\right)$$

$$\left(-\frac{4}{3}\right)$$

$$k = 28 \quad \{28\}$$

$$\underline{\text{ex}} \quad -x = -\frac{1}{2}$$

$$(-1)$$

$$(-1)$$

$$x = \frac{1}{2} \quad \left\{\frac{1}{2}\right\}$$

ex $9x + 2x = 121$

$$\frac{11x}{11} = \frac{121}{11}$$

$$x = 11 \quad \{11\}$$

ex $10x - 6x + 3x = -4$

$$\frac{7x}{7} = \frac{-4}{7}$$

$$x = -\frac{4}{7} \quad \left\{-\frac{4}{7}\right\}$$

ex If twice a # is divided by 5, the result is 4.

$$\frac{2x}{5} = 4$$

$$\left(\frac{5}{2}\right)\frac{2x}{5} = 4\left(\frac{5}{2}\right)$$

$$x = 10 \quad \{10\}$$

$$\begin{aligned} \underline{2.3} \quad \underline{\text{ex}} \quad 10p + 6 &= 12p - 4 \\ -10p \quad \quad -10p & \\ \hline 6 &= 2p - 4 \\ +4 \quad \quad +4 & \\ \hline 10 &= 2p \\ \frac{10}{2} \quad \frac{2p}{2} & \\ 5 &= p \quad \{5\} \end{aligned}$$

$$\begin{aligned} \underline{\text{ex}} \quad & 5(2m+3) - 4m = 8m + 27 \\ & 10m + 15 - 4m = 8m + 27 \\ & 6m + 15 = 8m + 27 \\ & \quad -8m \quad \quad -8m \\ & -2m + 15 = 27 \\ & \quad -15 \quad \quad -15 \\ & \quad \quad -2m = 12 \\ & \quad \quad \frac{-2m}{-2} = \frac{12}{-2} \\ & \quad \quad m = -6 \quad \{ -6 \} \end{aligned}$$

ex $3(6-4x) = 2(-6x+9)$

$$18 - 12x = -12x + 18$$

$+12x \quad +12x$

$\curvearrowright 18 = 18$
identity

{all real #s}

ex $6x - 4(x+1) = 2x + 4$

$$6x - 4x - 4 = 2x + 4$$

$$\begin{array}{r} 2x - 4 = 2x + 4 \\ -2x \quad \quad -2x \end{array}$$

$\curvearrowright -4 = 4$
contradiction

\emptyset or $\{ \}$

$$\begin{aligned} \underline{\text{ex}} \quad -\frac{5}{6}q - (q-1) &= \frac{1}{4}(-q+80) \\ \left[-\frac{5}{6}q - q + 1 = -\frac{1}{4}q + 20 \right] &\cdot 12 \quad \text{LCD} \\ -10q - 12q + 12 &= -3q + 240 \\ -22q + 12 &= -3q + 240 \\ +3q \quad \quad \quad +3q & \\ -19q + 12 &= 240 \\ -12 \quad \quad \quad -12 & \\ \hline -19q &= 228 \\ \hline -19 \quad \quad \quad -19 & \\ \hline q &= -12 \quad \quad \quad \{-12\} \end{aligned}$$

$$\underline{\text{ex}} \quad .3(x+15) + .4(x+25) = 25$$
$$(.3x + 4.5 + .4x + 10 = 25) \cdot 10 \quad \text{to rid decimals}$$

$$3x + 45 + 4x + 100 = 250$$

$$7x + 145 = 250$$
$$\quad -145 \quad -145$$

$$7x = 105$$
$$\quad \underline{\quad} \quad \underline{\quad}$$

$$x = 15 \quad \{15\}$$

ex Two #s have a sum of 26. One of the #s is r .

The other is $26 - r$

ex The product of 2 #s is -3 . One of the #s is m .

The other is $\frac{-3}{m}$

ex Chandler is b yrs old.

3 yrs ago: $b - 3$

5 yrs from now: $b + 5$